

## 2-Year Master's Program in Mathematics (NEP-2020)

### ALGEBRAIC TOPOLOGY

Master's Mathematics (2<sup>nd</sup> Semester)

Course Code: MMTHDAT226 (15 hours per credit)

**Continuous Assessment: Marks 30, Theory: Marks 70**

Total Credits: 04

Total Marks: 100

**Time Duration: 2½ hrs**

**Course Learning Outcomes(CLO's):** After successful completion of the course, the students will be able to:

**CLO1.** Understand concepts of path homotopy, deformation retracts, and basic topological constructions.

**CLO2.** Compute fundamental groups and apply them to classical theorems in topology and algebra.

**CLO3.** Analyze covering spaces and apply lifting theorems in topological contexts.

**CLO4.** Develop an understanding of simplicial complexes and compute simplicial homology using Mayer-Vietoris sequences.

#### **Unit-I**

Introduction to Homotopy, Paths and path homotopy, homotopy equivalence, relative homotopy, contractibility, deformation retracts. Strong deformability, Comb space and its contractibility.

#### **Unit-II**

Fundamental groups: construction of fundamental groups, fundamental group of circle. Application to Fundamental Theorem of Algebra, Brouwer's Fixed Point Theorem and the Borsuk-Ulam Theorem.

#### **Unit-III**

Covering spaces: covering spaces of  $S^1$  and  $S^1 \times S^1$ . Lifting: path and homotopy lifting, lifting properties, Lifting Criterion, regular covering spaces.

#### **Unit-IV**

Cell complexes, subcomplexes with examples. Simplicial complexes, barycentric subdivision, stars and links. Simplicial Homology, Mayer-Vietoris Sequences, long exact sequences.

#### **CLO-PLO Mapping Matrix (Strength version)**

| <b>CLO</b><br>↓ | <b>PLO</b><br>→ | PLO1     | PLO2     | PLO3     | PLO4        | PLO5        | PLO6        | PLO7        | PLO8       | Average<br>CLO |
|-----------------|-----------------|----------|----------|----------|-------------|-------------|-------------|-------------|------------|----------------|
| MMTHDAT226.1    |                 | 3        | 2        | 2        | 3           | 2           | 1           | 2           | 2          | <b>2.13</b>    |
| MMTHDAT226.2    |                 | 3        | 1        | 3        | 2           | 2           | 2           | 3           | 3          | <b>2.38</b>    |
| MMTHDAT226.3    |                 | 3        | 3        | 2        | 1           | 3           | 1           | 2           | 3          | <b>2.25</b>    |
| MMTHDAT226.4    |                 | 3        | 2        | 1        | 3           | 2           | 3           | 2           | 2          | <b>2.25</b>    |
| Average PLO     |                 | <b>3</b> | <b>2</b> | <b>2</b> | <b>2.25</b> | <b>2.25</b> | <b>1.75</b> | <b>2.25</b> | <b>2.5</b> | <b>2.25</b>    |

**Recommended Books:**

1. A. Hatcher, Algebraic Topology, Cambridge Univ. Press, Cambridge, 2002.
2. W. Fulton, Algebraic topology: A First Course, Springer-Verlag, 1995.
3. W. Massey, A Basic Course in Algebraic Topology, Springer-Verlag, Berlin, 1991.
4. J. J. Rotman, An Introduction to Algebraic Topology, Springer (India), 2004.
5. J. R. Munkres, Elements of Algebraic Topology, Addison-Wesley, 1984.
6. S. Deo, Algebraic Topology, A Primer, Springer.